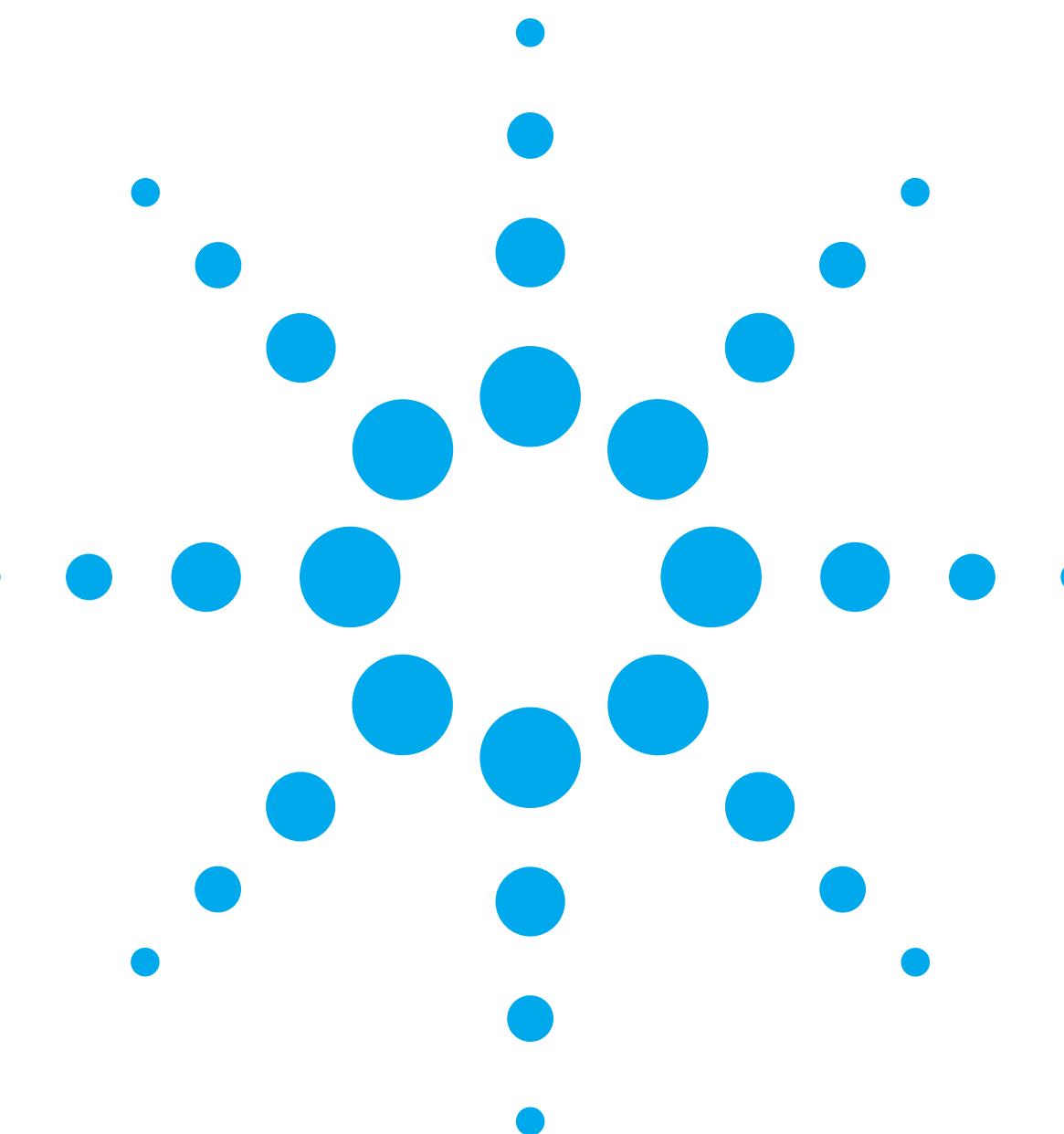


RF & Microwave References



S-Parameter/Return Loss/Smith Chart

S-parameters (scattering parameters) are a convention for characterizing RF & microwave devices, consisting of reflection and transmission coefficients—familiar concepts to designers. Transmission coefficients are commonly referred to as gains or attenuations, reflection coefficients relate to return losses and VSWRs (voltage standing wave ratios).

Conceptually, "s" parameters are like "h", "y", or "z" parameters because they describe the inputs and outputs of a black box. The inputs and outputs are in terms of power for "s" parameters; for "h", "y", and "z" parameters, they are voltages and currents.

Using the convention that "a" is a signal into a part and "b" is a signal out, the figure below helps to explain "s" parameters.

In this figure, "a" and "b" are the square roots of power; $(a_1)^2$ is the power incident at port 1 and $(b_2)^2$ is the power leaving port 2. The diagram shows the relationship between the "s" parameters and the "a"s and "b"s. For example, a signal, a_1 , is partially reflected at port 1; the rest of the signal is transmitted through the device and out of port 2. The fraction of a_1 that is reflected at port 1 is s_{11} ; the fraction of a_1 that is transmitted is s_{21} . Similarly, the fraction of a_2 that is reflected at port 2 is

s_{12} and the fraction a_2 is transmitted. The signal, b_1 , leaving port 1 is the sum of port 1 and the fraction of a_1 that is reflected at port 1 and the fraction of a_2 that is transmitted from port 2. Thus, the outputs can be related to the inputs by the equations:

$$b_1 = s_{11}a_1 + s_{21}a_2$$

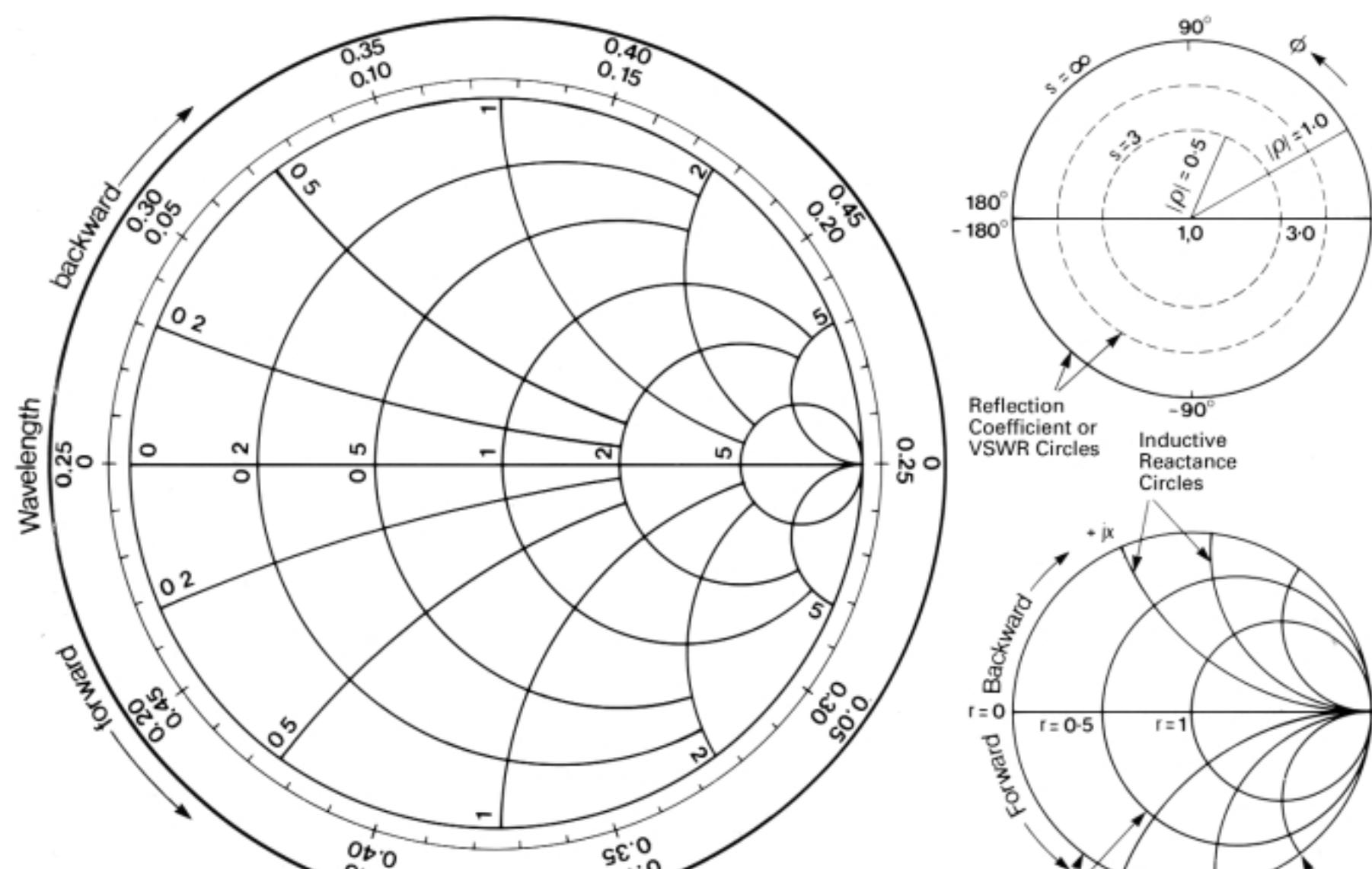
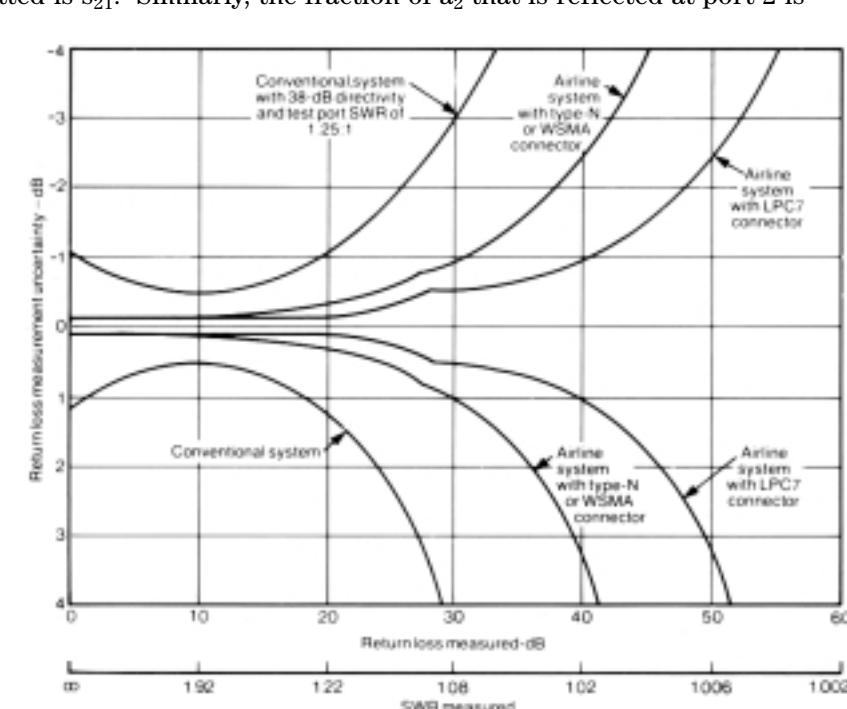
$$b_2 = s_{21}a_1 + s_{22}a_2$$

when $a_2 = 0$

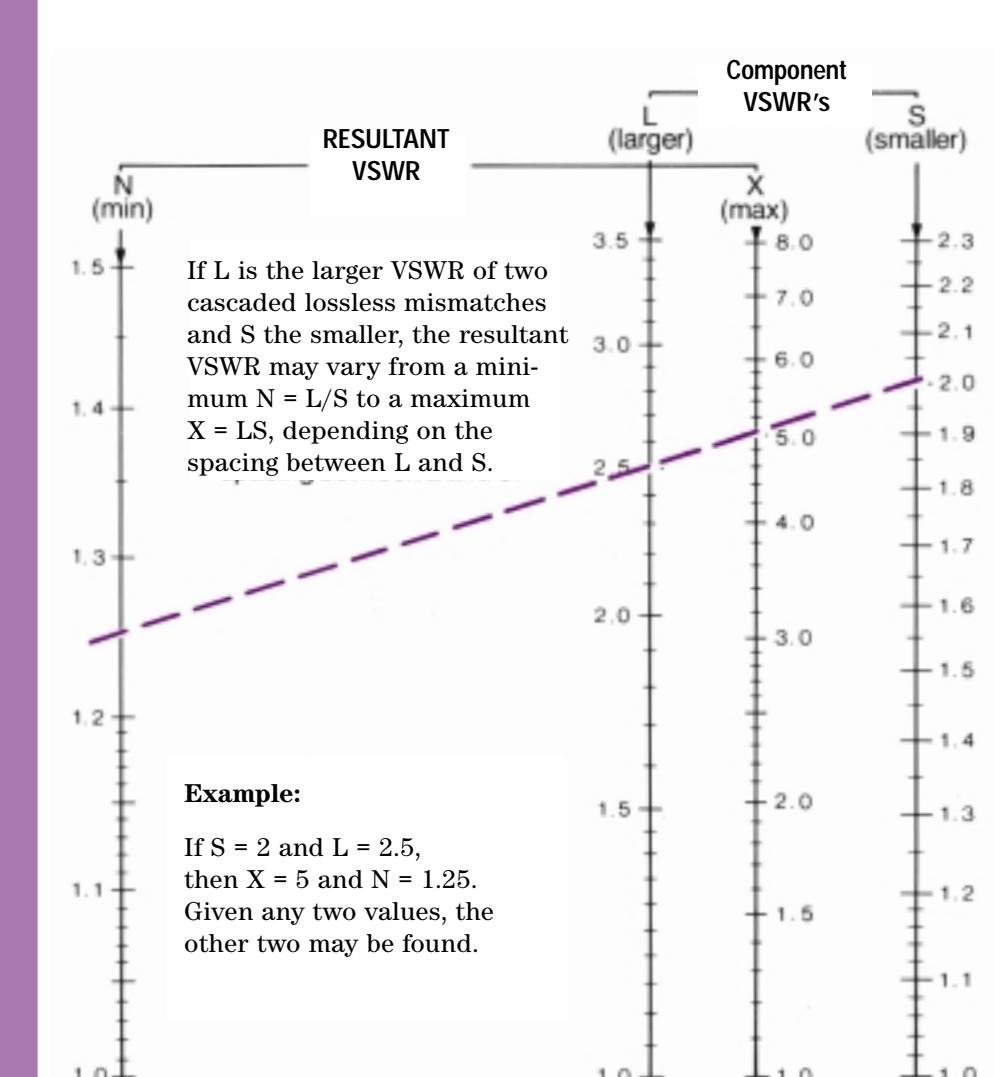
$$s_{11} = \frac{b_1}{a_1} \quad s_{21} = \frac{b_2}{a_1}$$

and when $a_1 = 0$

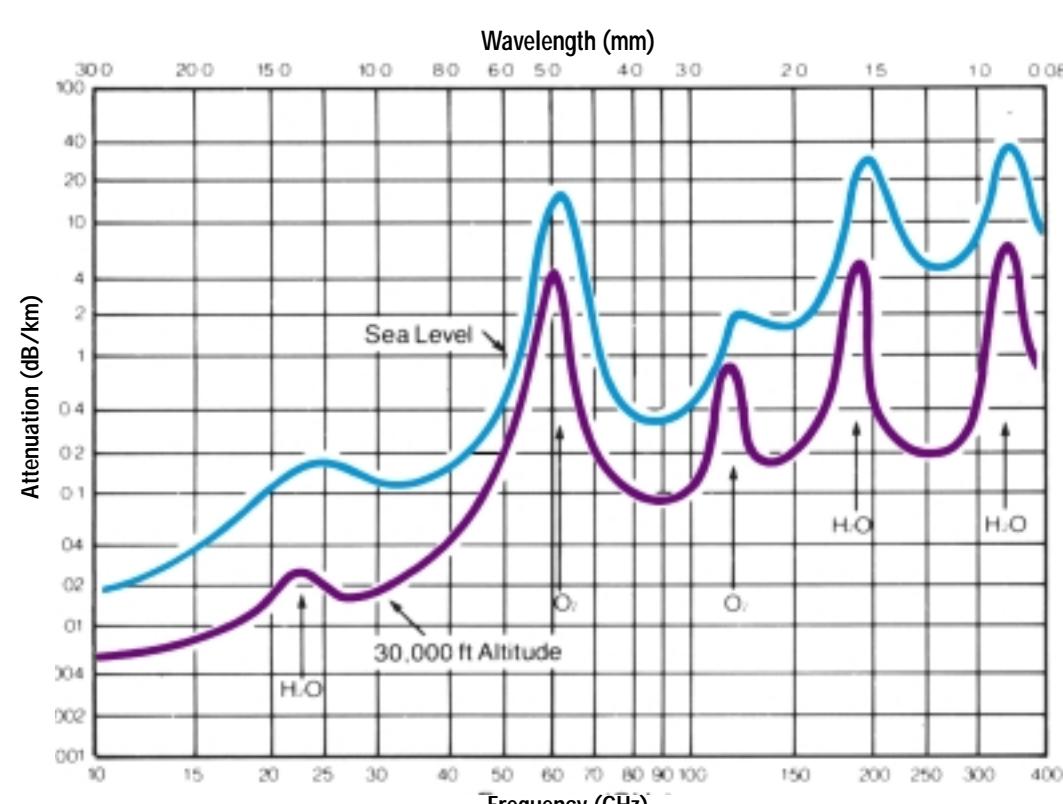
$$s_{22} = \frac{b_2}{a_2} \quad s_{12} = \frac{b_1}{a_2}$$



Maximum and Minimum Resultant VSWR from Two Mismatches

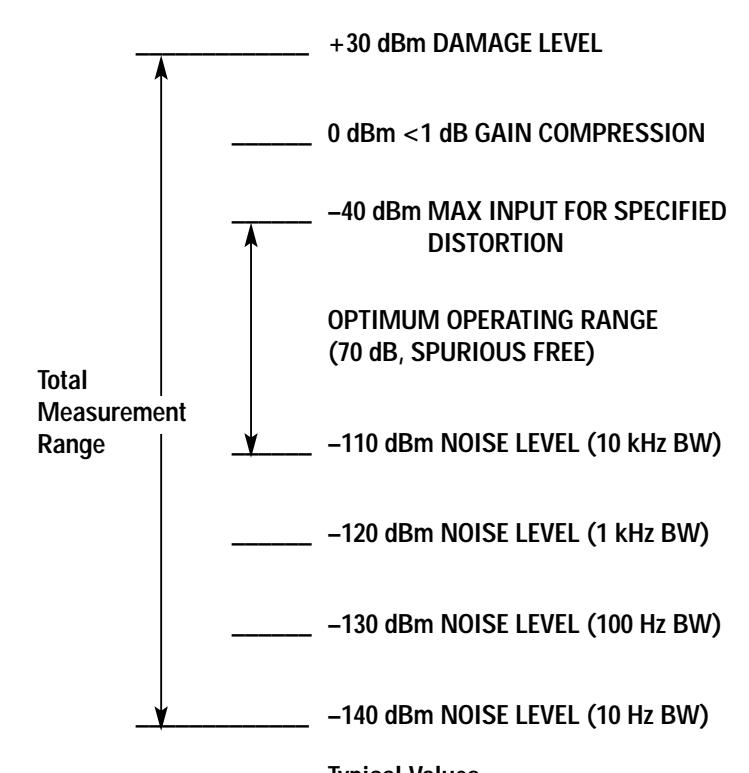


Millimeter-Wave Transmission Attenuation Curves

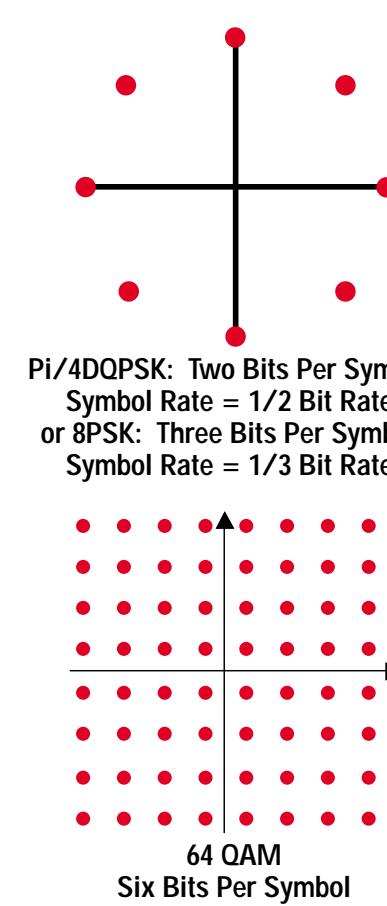
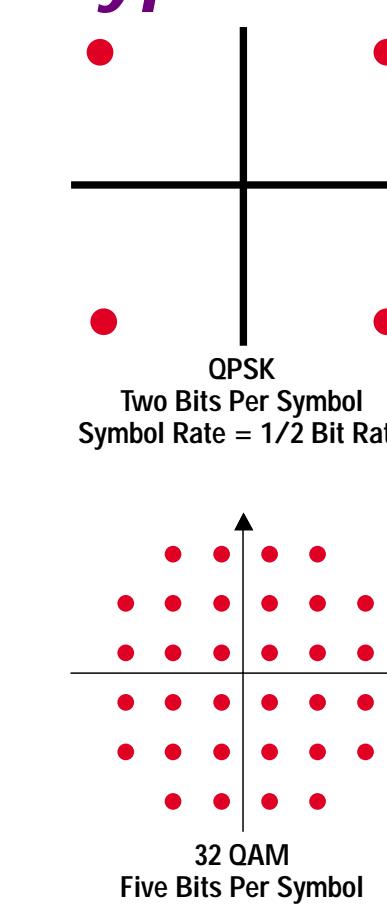
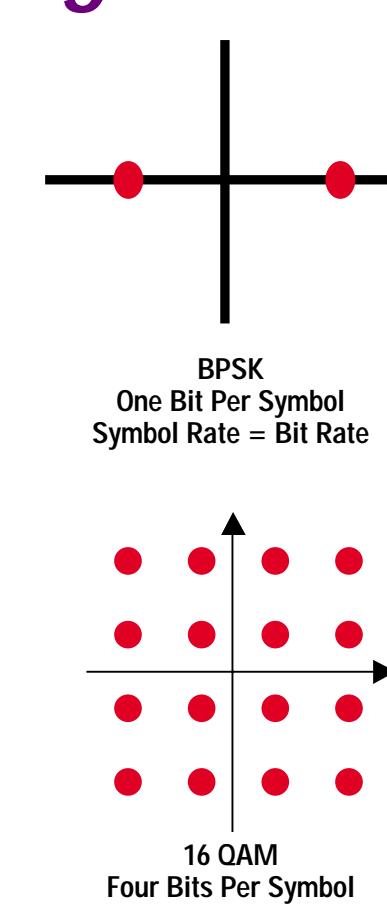


The atmospheric attenuation of mm-wave signals varies greatly, allowing for long-range exploitation by operating in the windows at 35, 94, 140, and 220 GHz, or for short-range, intercept-resistant communications at 44 to 65 GHz.

Spectrum Analyzer Display Range



Digital Modulation Type and Constellation



16 QAM (Four Bits Per Symbol, Symbol Rate = 1/4 Bit Rate)

32 QAM (Five Bits Per Symbol, Symbol Rate = 1/5 Bit Rate)

64 QAM (Six Bits Per Symbol, Symbol Rate = 1/6 Bit Rate)

Microwave Formulae

$$\text{Wavelength } (\lambda) = \frac{3 \times 10^8}{f}$$

$$\lambda(\text{meters}) = \frac{3 \times 10^{-9}}{f}$$

where f = frequency (hertz)

dB (Power and Voltage)

$$\text{dB}_{\text{power}} = 10 \log_{10} \frac{P_1}{P_2}$$

$$\text{dB}_{\text{voltage}} = 20 \log_{10} \frac{E_1}{E_2}$$

where P_1 & P_2 = system powers
 E_1 & E_2 = system voltages

Characteristic Impedance (Z_0) of RF Cable

$$Z_0 = \frac{138}{\sqrt{\epsilon_r}} \log_{10} \frac{D}{d}$$

where ϵ_r = relative dielectric constant
D = inside diameter of outer conductor
d = outside diameter of inner conductor

Velocity Factor

$$v = \frac{1}{\sqrt{\epsilon_r}} \times 100$$

where ϵ_r = relative dielectric constant

Noise Figure (NF_{av})

$$NF_{av} = 10 \log_{10} \frac{S_o/N_o}{S_i/N_i}$$

Where NF_{av} = noise figure (dB)
S_i/N_i = input signal-to-noise ratio
S_o/N_o = output signal-to-noise ratio

Reflection Coefficient ρ

$$\rho = \frac{VSWR - 1}{VSWR + 1}$$

where VSWR = Voltage Standing Wave Ratio

Return Loss in dB

$$dB = 20 \log_{10} |\rho|$$

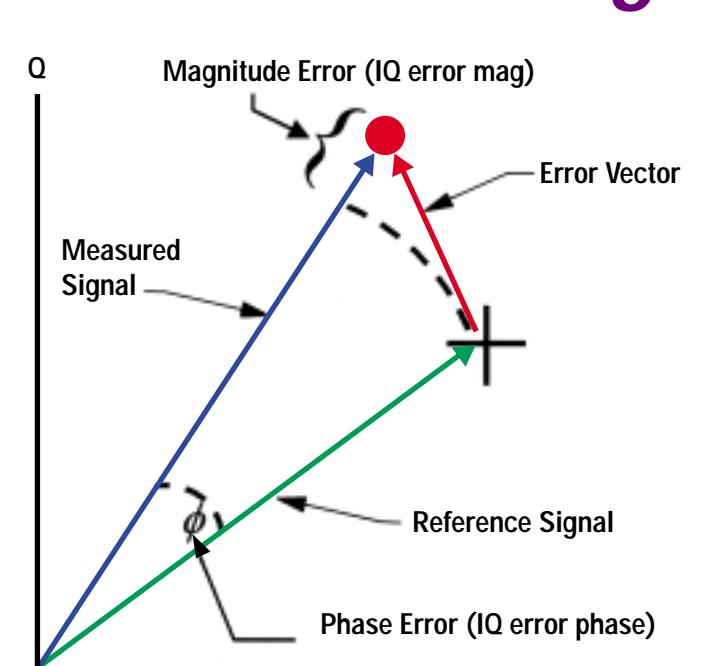
where ρ = reflection coefficient

VSWR

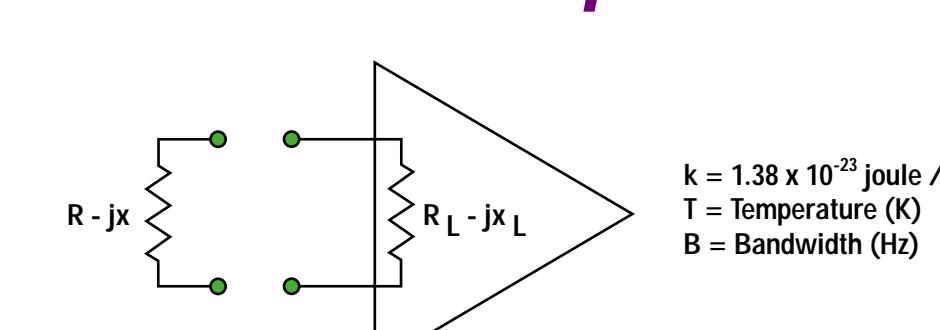
$$VSWR = \frac{1 + \rho}{1 - \rho}$$

where ρ = reflection coefficient

Modulation Quality: Error Vector Magnitude



Noise Power at Standard Temperature



$$\text{Noise Figure (NF}_{av}\text{)}$$

$$NF_{av} = 10 \log_{10} \frac{S_o/N_o}{S_i/N_i}$$

Where NF_{av} = noise figure (dB)
S_i/N_i = input signal-to-noise ratio
S_o/N_o = output signal-to-noise ratio

Available Noise Power*

$$P_{av} = KT_B$$

$$\text{At } 290K_{av} = 4 \times 10^{-21} \text{ W/Hz} = -174 \text{ dBm/Hz}$$

In deep space $KT = -198 \text{ dBm/Hz}$

* Noise figure is defined when input is terminated at 290 Kelvins.

